

Link Scheduling

Dr. Yeali S. Sun

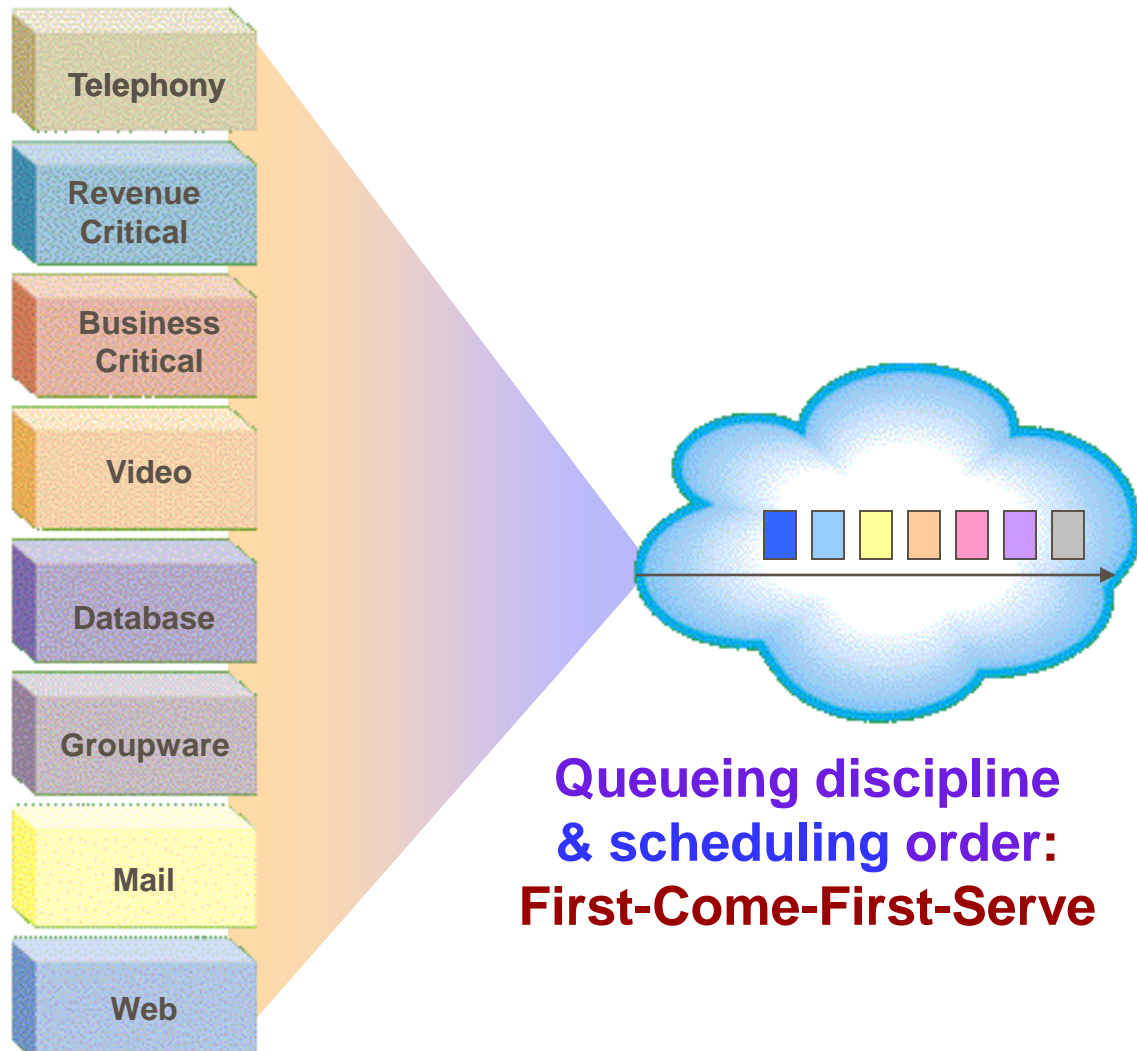
National Taiwan University

Link Scheduling in Integrated Services Networks (1/4)

- Traditionally, the *flexibility* of data networks has been *traded off* with the *performance guarantees* given to its users, e.g.,
 - The **telephone network** provides *good* performance guarantees but *poor flexibility*
 - **Packet switched networks** are more flexible but only provide marginal performance guarantees.
 - Traffic characteristics
 - Integrated services networks will carry *a wide range of traffic types* and must be able to provide performance guarantees to real-time sessions such as voice and video.
- > The problem is how to reconcile these apparently conflicting demands when the **short-term demand** for link usage frequently exceeds the usable **capacity**.

Today's Internet

- Performance of *mission critical* applications are threatened
- *Uncontrolled* use of bandwidth in WAN
- Need technologies to manage link sharing and guarantee QoS on a per interface basis
- Need *automated* QoS management



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Link Scheduling in Integrated Services Networks (2/4)

- Schedule packet transmissions of the **sessions** (flows) at a single node.
- Packet delay in the network can be expressed as the sum of the processing, queueing, transmission, and propagation delays
- The **focus** is on how to **limit *queueing delay***.
- Wish to guarantee ***worst-case packet delay***.

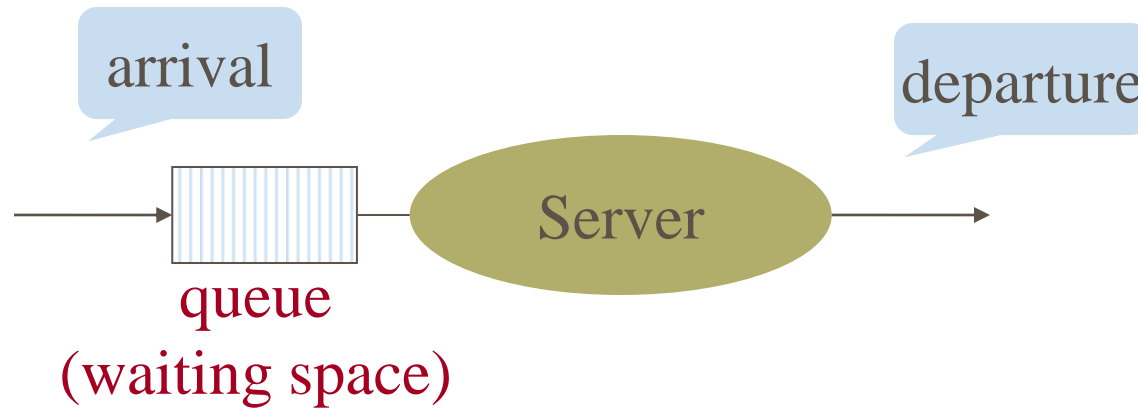
Link Scheduling in Integrated Services Networks: requirements (3/4)

- Treat users **differently**, in accordance with their desired **QoS**.
- Flexibility should not compromise the **fairness** of the scheme (e.g., in priority-based scheduling).
- Performance guarantees should be analyzable.

Link Scheduling in Integrated Services Networks (4/4)

- An important approach is to *combine* the use of a *packet service discipline* based on Generalized Processor Sharing (GPS) and Leaky Bucket rate control to provide
 - *flexible, efficient, and fair* use of the links, and
 - *performance guarantees*
- **Weighted Fair Queueing (WFQ)** is the packet version of GPS which closely approximates GPS.
 - a way of rate-based flow control

A Link is modeled as a Queueing Server



■ Arrival process

- customers to be served
- Inter-arrival time distribution

■ Queue

- finite or infinite capacity

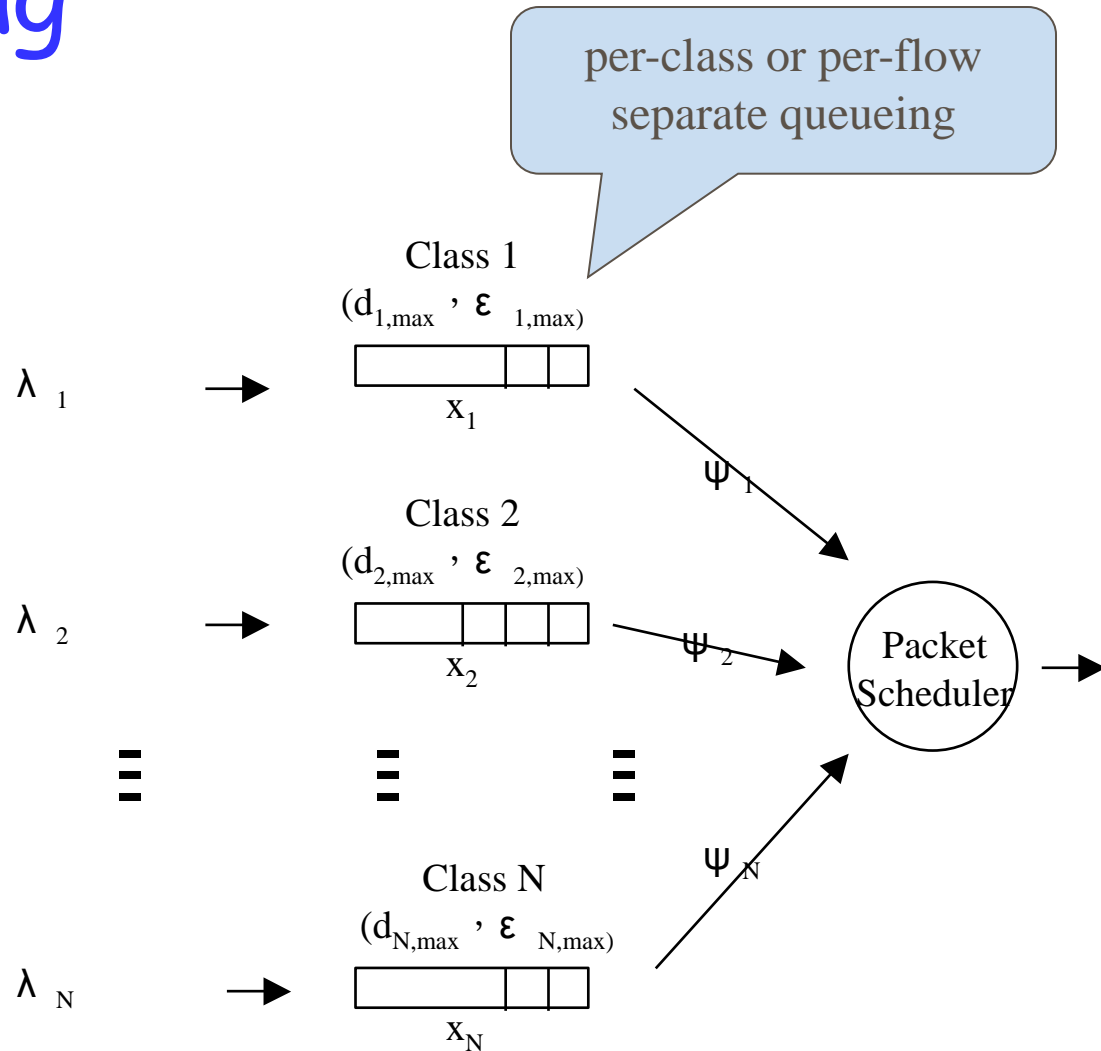
■ Service time distribution

- Workload
- Queueing discipline
 - FIFO, LIFO, priority, etc.
- Number of servers

-> Nobody likes to wait in line.

Fair Queueing

- Consider N queues
- The goal is to provide *flexible*, *efficient* and *fair* use of the links
 - Flexible: meeting QoS of *all* queues
 - Efficient: *maximal* link utilization (work conserving)
 - Fair: *excess* bandwidth sharing and assignment



Generalized Processor Sharing (GPS)

- **Head-of-line Processor Sharing service (PS)**
 - A **separate** FIFO queue for **each** *session* sharing the same link
 - During any time interval, if there are exactly N packets at the head of the queues, each receives a $1/N$ of the link speed
- **GPS is a generalized form of PS**

GPS Server (1/7)

- Consider a **work-conserving** server with rate r serving N sessions
 - *Work-conserving* means the server (the link) will **not** be idle if a packet **waiting** for transmission
- Each **session** i is assigned a fixed real-valued positive parameter ϕ_i .

GPS Server (2/7)

- $\phi_1, \phi_2, \dots, \phi_N$ are *relative amount of service to each session* such that let $S_i(\tau, t)$ be the amount of session i traffic *served* during an interval $[\tau, t]$ then

$$\frac{S_i(\tau, t)}{S_j(\tau, t)} \geq \frac{\phi_i}{\phi_j}$$

- assuming any session i that is continuously backlogged in the interval $[\tau, t]$

GPS Server (3/7)

- Sum up all sessions j

$$S_i(\tau, t) \sum_j \phi_j \geq (t - \tau) r \phi_i$$

$$S_i(\tau, t) \phi_j \geq S_j(\tau, t) \phi_i$$

$$S_i(\tau, t) \sum_j \phi_j \geq \phi_i \sum_j S_j$$

$$S_i(\tau, t) \sum_j \phi_j \geq \phi_i (t - \tau) r$$

$$g_i \geq \frac{\phi_i}{\sum_j \phi_j} r$$

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GPS Server (4/7)

- Let $B_{GPS}(\tau)$ be the set of **backlogged** sessions at time τ
- If $B_{GPS}(\tau)$ remains **unchanged** during the interval, the service rate of session i during the interval will be exactly

$$g_i = \frac{\phi_i}{\sum_{j \in B_{GPS}(\tau)} \phi_j} r$$

- where r is the rate of the link

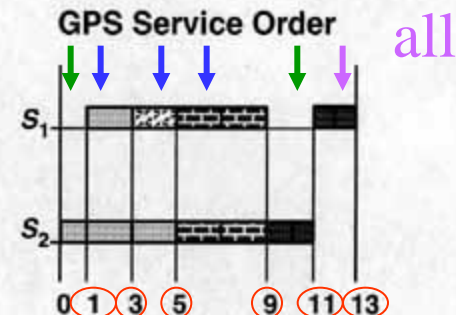
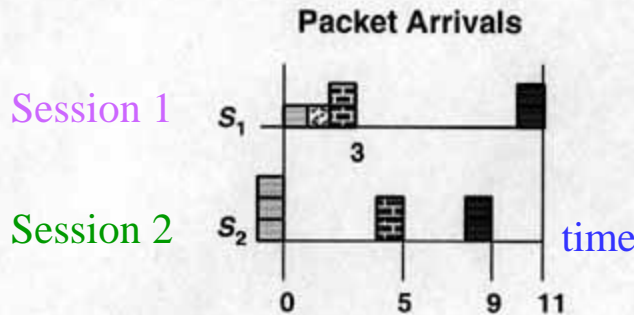
GPS Server: Fluid-flow (bit-by-bit) scheme (5/7)

Concurrent (shared) or Full possession!

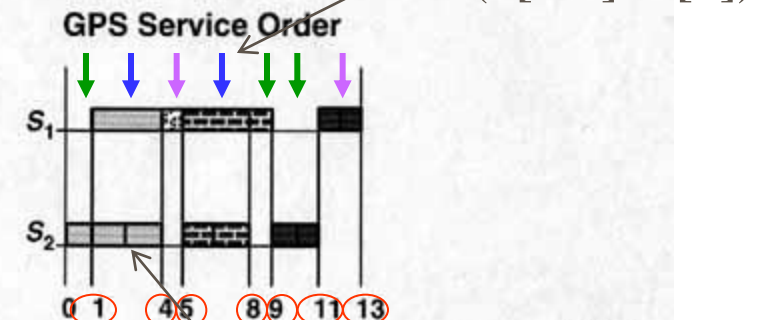
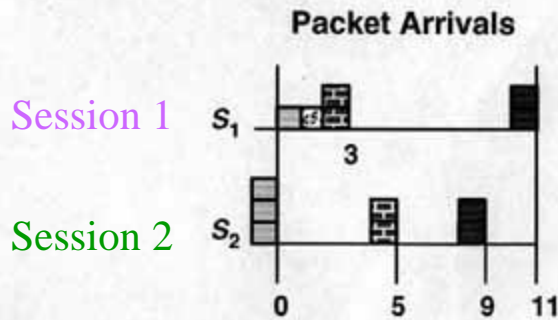
- Consider a server with rate 1 serving 2 sessions
- Assume a packet has arrived only after its last bit has arrived

$$- \phi_1 = \phi_2$$

all sharing



$$- 2\phi_1 = \phi_2$$



Variable length packets

$$3 \text{ units } (2/(2/3)=3)$$

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GPS Server: properties (6/7)

■ Throughput guarantee

- Define r_i be the session i average rate
- As long as $r_i \leq g_i$, the session is guaranteed a throughput of ρ_i , *independent of the demands of the other sessions.*

■ Delay bound

- The delay of an arriving session i is bounded as a function of the session i **queue length, independent** of the queues and arrivals of the **other** sessions.
- Schemes such as FCFS, LCFS, and strict priority do not have this property.

GPS Server: properties (7/7)

- By **varying the ϕ_i 's**, the scheme has the flexibility of treating the sessions in a variety of ways, e.g.,
 - When all ϕ_i 's are equal \rightarrow uniform processor sharing
 - When combined average rate of the sessions is less than r , any assignment of positive yields a **stable** system.
 - A high-bandwidth-delay-insensitive session i can be assigned g_i much less than its average rate, thus allowing for better treatment of the other sessions.
- **Worst-case delay guarantee**
 - When sources are constrained by leaky buckets.
 - **Attractive** for sessions with **real-time** constraints like voice and video

Packet Generalized Processor Sharing (PGPS)

■ GPS

- **Fluid-flow (bit-by-bit)** scheme (concurrency)
- Cannot be applied to packet-based networks

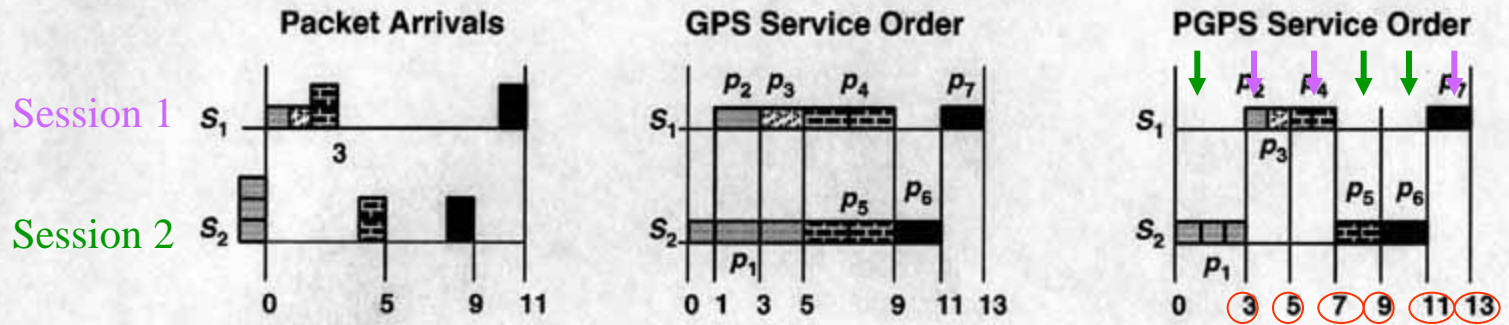
■ PGPS

- A **packet** approximation algorithm of GPS
- Packet-by-packet scheme
- **a.k.a Weighted Fair Queueing (WFQ)**

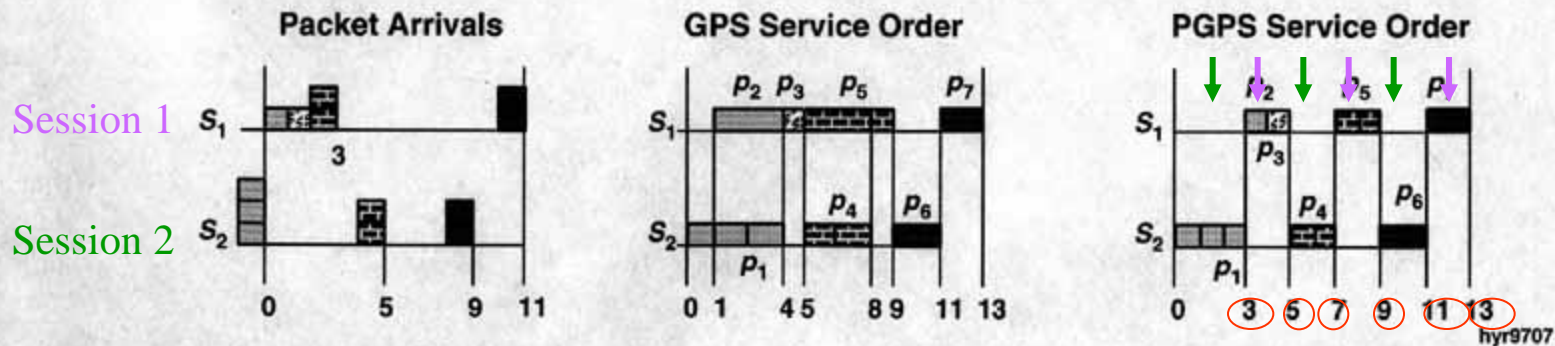
PGPS Server: packet version of GPS

- Consider a server with rate 1 serving 2 sessions
- Assume a packet has arrived only after its last bit has arrived

$$-\phi_1 = \phi_2$$



$$-2\phi_1 = \phi_2$$



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Packet Generalized Processor Sharing (PGPS): Properties

1. *Weighted* fair allocation of bandwidth
2. *Minimum* bandwidth guarantee
3. *Flow isolation*
 - Protection from misbehaving sources such as UDP flows that do not reduce rate when congestion occurs
4. *Guaranteed bounded delay services*
 - Provided sources are *leaky bucket constrained*.

WFQ: Packet Scheduling

- WFQ tries to *emulate* GPS.
- Consider *two* queueing systems
 - one using the GPS discipline and
 - one using the PGPS discipline
- **Determine which packet to server next?**
 - **Serve packets in increasing order of d_p^{GPS}**
 - d_p^{GPS} : the departure time of packet p under *GPS*

WFQ: Packet Scheduling (cont'd)

- Under GPS, when the system is ready to choose the next packet to transmit, the **next packet to depart under GPS** may not have arrived at the packet system yet.
 - Fluid model vs. packet model
- Waiting for it may cause system **idle** under non-empty system, i.e. non-work conserving.

PGPS: Virtual Time - notations

- Assume server works at rate 1
- Event
 - a *packet arrival* and *departure* from the *GPS server*
- t_j : the time at which the j^{th} event occurs
 - assume $t_1=0$
- \mathbf{B}_j : the set of sessions that are backlogged in the interval (t_{j-1}, t_j)
- $\mathbf{V}(\mathbf{t})$: *zero* for all times when the server is *idle*

PGPS: Virtual clock vs. Actual clock (1/5)

- The curve function is changing from one interval to another

- An interval is (t_{j-1}, t_j) , $j=2, 3, \dots$

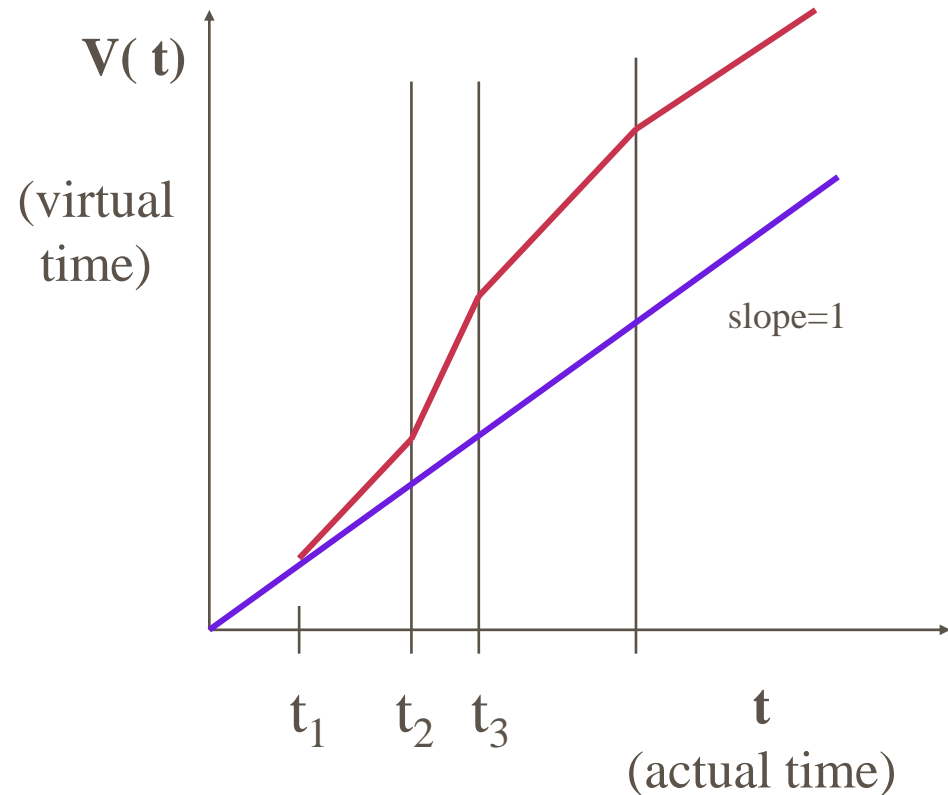
- The slope is $\frac{1}{\sum_{j \in B_{GPS}} \phi_j}$

- Consider a **busy period** that begins at time zero

- $V(t)$ evolves as follows:

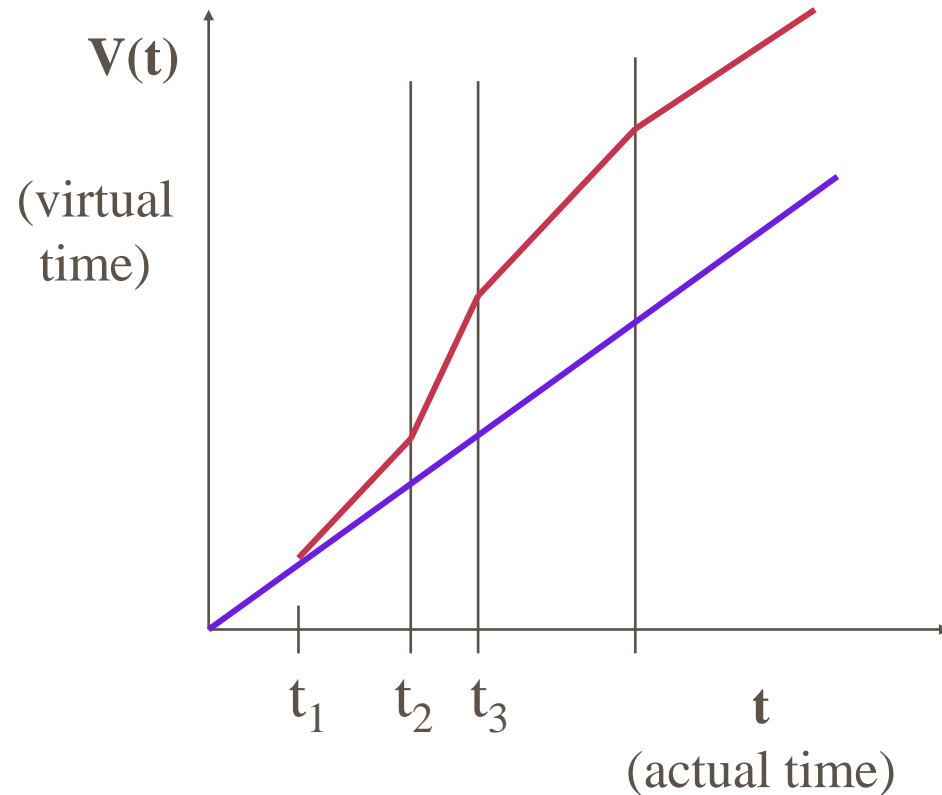
- $V(0) = 0$

- $V(t_{j-1} + \tau) = V(t_{j-1}) + \tau / \sum \phi_j$,
 $\tau \leq t_j - t_{j-1}$, $j=2, 3, \dots$



PGPS: Virtual clock vs. Actual clock (2/5)

- $V(t)$ changes at the rate of $1/\sum\phi_j$
- For a backlogged session
 - When $\sum\phi_j < 1$, it seems that the “corresponding” server becomes **faster**, from ϕ_i to $\phi_i * 1/\sum\phi_j$
- For individual backlogged sessions, the portion of service rate received **increases**.



PGPS: Virtual clock vs. Actual clock (3/5)

- $1/\sum \phi_j$ represents the “current” service rate *from the backlogged sessions’ point of view*
- Each backlogged session receives service at **rate $\phi_i * (\partial V(t_j + \tau) / \partial \tau)$**
- $V(t)$ is a non-decreasing function
- Packet service order of a session is FIFO

PGPS: Virtual clock vs. Actual clock (4/5)

- $a_{i,k}$: the **(actual) arrival time** of the k^{th} packet of session i
- $V(a_{i,k})$: the virtual time of $a_{i,k}$
- Need to obtain a correspondence of a *packet arrival time* and *departure time* in the **virtual time domain**
- $S_{i,k}$: the virtual time that packet k of session i begins its **service**
- $F_{i,k}$: the **virtual finishing time** of $a_{i,k}$
- We have
 - $S_{i,k} = \max\{F_{i,k-1}, V(a_{i,k})\}$
 - $F_{i,k} = S_{i,k} + L_{i,k} / \phi_i$

where $L_{i,k}$ is the packet length

and $L_{i,k} / \phi_i$ is the “presumed” service time, i.e. the *worst-case service time*

PGPS: Virtual Finishing Time (5/5)

- When a packet arrives, virtual clock is updated and the packet is stamped with its **virtual finishing time** ($F_{i,k} = \max\{F_{i,k-1}, V(a_{i,k})\} + L_{i,k}/\phi_i$)
- Server is work-conserving and serves packets in an ***increasing order of virtual finishing time***
- Virtual times are updated when an arrival or departure occurs (***rate change***).
- The system must keep track of the set of $B_j(t)$ (***the set of backlogged sessions at time t***).

Relationship between a fluid GPS and its corresponding WFQ systems

- In terms of queueing delay, a packet will finish its service in a WFQ system **later** than in the GPS system by **NO more than** the transmission time of **one** maximum size packet
- In terms of total number of bits served for a session, a WFQ system **does NOT fall behind** a corresponding GPS system by **more than one** maximum size packet.

Summary

- Fair queueing to support QoS
- WFQ
 - Approximating GPS
 - **Minimum throughput guarantee**
 - **Flow isolation**
 - **Delay bound guarantee**
 - **Weighted Fairness**

Other Scheduling Algorithms

- WF2Q
- WF2Q-M
- Deficit Round Robin (DRR)
- etc.

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